

Implementation of Complex Vedic Multiplier using Three Multiplier and Kogge Stone Adder Technique

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Abstract- The main objective of this research paper is to design architecture for complex Vedic multiplier by rectifying the problems in the existing method and to improve the speed by using the kogge stone adder with the help of hybrid square technique. The Vedic multiplier algorithm is normally used for higher bit length applications and ordinary multiplier is good for lower order bits. These two methods are combined to produce the high speed multiplier for higher bit length applications. The problem of existing architecture is reduced by removing bits from the remainders. The proposed algorithm is implementation Xilinx software with Vertex-7 device family.

Keywords- Vedic Multiplier, Complex Multiplier, Hybrid Square Kogge Stone Adder, Xilinx Software.

I. INTRODUCTION

Arithmetic is the oldest and most elementary branch of Mathematics. The name Arithmetic is derived from the Greek word "arithmos". Arithmetic is used by almost everyone, for tasks ranging from simple day to day work. As a result, the need for a faster and efficient Arithmetic unit in computers is the interesting topic over decades. The four basic operations in elementary arithmetic are addition, subtraction, multiplication and division.

Multiplication is the basic mathematical operation of scaling one number by another. Multiplication is used in today's engineering field covering many Digital Signal Processing (DSP) applications such as convolution, Fast Fourier Transform (FFT), filtering and in Arithmetic Logic units of a microprocessor, microcontroller and most of the Embedded controllers.

The demand for high speed processing has been increasing as a result of expanding computer and signal processing applications. Higher throughput arithmetic operations are essential to achieve the desired performance in many real-time signal and image processing applications.

One of the key arithmetic operations in such applications is multiplication and the development of faster multiplier circuit has been a subject of interest over decades. Reducing the time delay and power consumption are very essential requirements for many applications.

Parallel multiplication is used to meet out the current requirement. Two types of parallel multiplications are array multiplication and tree multiplication. The basic multiplier is a simple array multiplier and it is designed based on shift- and – add operation. One of the examples for array multiplication is the Braun multiplier and is designed for unsigned binary numbers. For tree structure Wallace multiplier is designed and it is also for an unsigned binary numbers.

In the array multiplication, for signed numbers Baugh – Wooley, Booth Multiplier and Modified Booth Algorithm (MBA) are used. Dadda is another type of multiplier based on tree structure and is used for the multiplication of the signed numbers. These conventional binary multipliers for unsigned numbers are considered for comparison. Vedic mathematics is the system of mathematics followed in ancient India and mainly deals with Vedic mathematical formulae and their applications to

various branches of mathematics. The word 'Vedic' is derived from the word 'Veda' which means the storehouse of all knowledge.

Vedic mathematics was reconstructed from the ancient Indian scriptures (Vedas) by Sri Bharati Krishna Tirthaji (1884- 1960), after his eight years of research on Vedas. According to his research, Vedic mathematics is mainly based on sixteen principles or word-formulae and thirteen sub-corollaries which are termed as Sutras. This is a very interesting field and presents some effective algorithms which can be applied to various branches of Engineering such as Computing and Digital Signal Processing.

Vedic mathematics reduces the complexity in calculations that exist in conventional mathematics. Generally there are sixteen sutras available in Vedic mathematics.

Among them only two sutras are applicable for multiplication operation. They are Urdhava Triyakbhyam sutra (literally means vertically and crosswise) and Nikhilam Sutra (literally means All from 9 and last from 10). Urdhava-Triyakbhyam is a generic method for multiplication. The logic behind Urdhava Triyakbhyam sutra is very much similar to the ordinary array multiplier. Here the binary implementation of this algorithm is derived based on the same logic used for decimal numbers. The binary implementation of Nikhilam Sutra is not yet successful.

This is a special case in multiplication. Another algorithm used to simplify the multiplication process is Karatsuba algorithm. This Karatsuba algorithm uses a divide-and-conquer approach where it breaks down the inputs into Most Significant half and Least Significant half and this process continues until the operands are of 8-bits wide. Karatsuba algorithm is best suited for operands of higher bit length. But at lower bit lengths, it is not as efficient as it is at higher bit lengths. This method was discovered by Anatoli Karatsuba in 1962. It reduces the number of multipliers required, by replacing the multiplication operations by addition operations.

Addition operations are faster than multiplications and hence the speed of the multiplier is increased. As the amount of bits increase, the efficiency of the multiplier will also increase.

In this research paper, a novel architecture of complex multiplier is designed using hybrid square kogge stone adder.

II. TYPES OF MULTIPLIER

Multipliers play an important role in today's digital signal processing and various other applications. Essential design targets of multiplier include high speed, low power consumption, regularity of layout and hence less area or even combination of them in one multiplier are required thereby making them suitable for various VLSI implementations.

Most multiplication techniques can be classified as Array multipliers and Tree multipliers. A detailed discussion on the different types of multipliers is done in the following sections.

1. Array Multipliers:

Array multipliers can be implemented by directly mapping the manual multiplication into hardware. The partial products are accumulated by an array of adder circuits. An $n \times n$ array multiplier requires $n(n-1)$ adders and n^2 AND gates.

2. Carry Save Array Multiplier:

The carry-save array multiplier uses an array of carry-save adders for the accumulation of partial product. It uses a carry-propagate adder for the generation of the final product. This reduces the critical path delay of the multiplier since the carry-save adders pass the carry to the next level of adders rather than the adjacent ones.

3. Wallace Tree Multiplier:

C. S. Wallace (1964) propounded a fast technique to perform multiplication. A Wallace tree multiplier offers faster performance for large operands. Unlike an array multiplier the partial product matrix for a tree multiplier is rearranged in a tree-like format, reducing both the critical path and the number of adder cells needed.

4. Dadda Multiplier:

Dadda multiplier is a hardware multiplier designed similar to Wallace multiplier. Unlike Wallace multipliers that perform reductions as much as possible on each layer, Dadda multipliers do as few reductions as possible. Due to this, Dadda multipliers have less expensive reduction phase, but the numbers may be a few bit longer, thus requiring

slightly bigger adders. This implies that fewer columns are compressed in the initial stages of the column compression tree, and more columns in the later levels of the multiplier.

5. Booth Wallace Tree Multipliers:

The use of Booth’s algorithm, in multiplication presents an efficient solution that suits the demands of high-speed multipliers, which also need to be efficient in terms of hardware design/area complexity.

In this multiplier, the partial products are generated using the Booth method, while their summation is done using Wallace tree structure. This compresses the addition process. The adder is used in adder accumulator configuration, where the multiplication result is added every time to the partial product register.

Table 1. Comparison of Multiplier.

Types of Multiplier	Delay/ Increase in bit size	Structure/ Complexity	Area	Speed
Array	Linear	Regular/ Low	High	Low
Wallace	Logarithmic	Irregular/ High	High	High
Dadda Tree	Logarithmic	Irregular/ High	High	High
Booth	Non-linear	Regular/ Medium	Low	Medium

III. VEDIC MULTIPLIER

Vedic multiplier and hybrid square Kogge Stone adder can compare with conventional method which is computed by Vedic multiplier, full adder and half adder. Proposed technique provides less path delay and less area. Input sequence of Conventional method is much more than to proposed method, however proposed method has less propagation delay. Area and propagation delay can be reduced by the aid of hybrid square Kogge Stone adder. This adder will be designed like as ripple carry adder.

Logic Diagram of Vedic Multiplier using Kogge Stone Adder is shown in figure 1. Eventually, all the designing levels of digital system or IC’s Packages

depend on number of gates in a single chip that is also called bottom up approach. Modified KS adder can be reduced regarding the area or number of gates. If we remove the first XOR gate from modified KS adder nothing will be changed for result but area and propagation delay will be reduced.

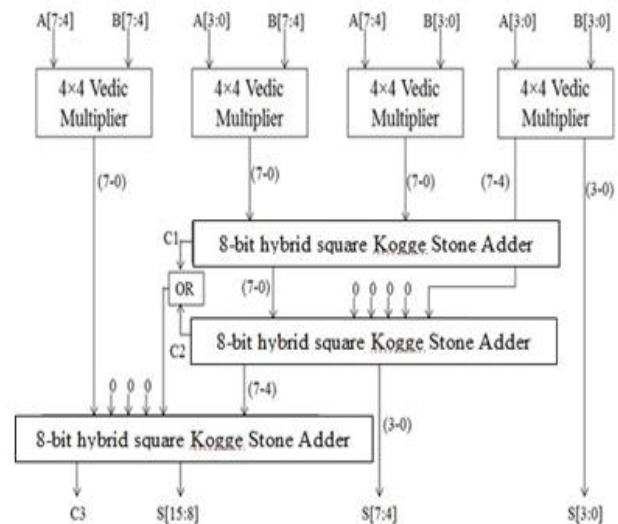


Fig 1. 8-bit Vedic Multiplier using Hybrid Square Kogge Stone Adder.

1. Hybrid Square Kogge Stone Adder:

The complete functioning of KSA can be easily comprehended by analyzing it in terms of three distinct parts:

1.1 Preprocessing: This step involves computation of generate and propagate signals corresponding too each pair of bits in A and B. These signals are given by the logic equations below:

$$P_i = A_i \text{ xor } B_i \tag{1}$$

$$G_i = A_i \text{ and } B_i \tag{2}$$

1.2 Carry look ahead network: This block differentiates KSA from other adders and is the main force behind its high performance. This step involves computation of carries corresponding to each bit.

$$C_i = G_i \text{ or } (P_i \text{ and } C_{i-1}) \tag{3}$$

1.3 Post processing: This is the final step and is common to all adders of this family (carry look ahead). It involves computation of sum bits. Sum bits are computed by the logic given below:

$$S_i = P_i \text{ xor } C_{i-1} \tag{4}$$

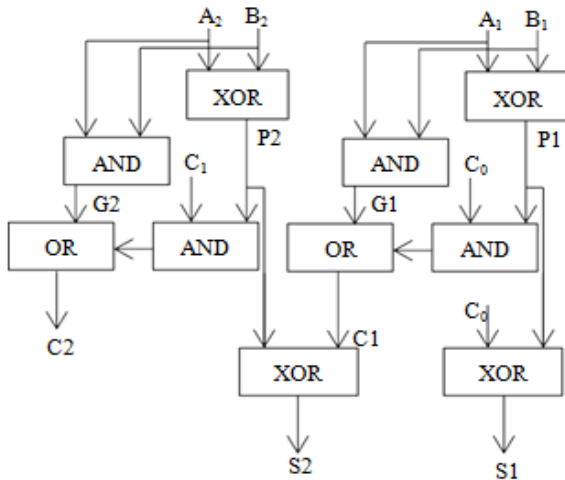


Fig 2. 2-bit Hybrid Square Kogge Stone Adder.

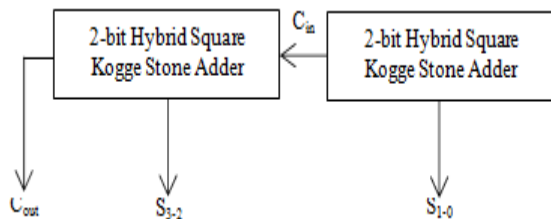


Fig 3. 4-bit Hybrid Square Kogge Stone Adder.

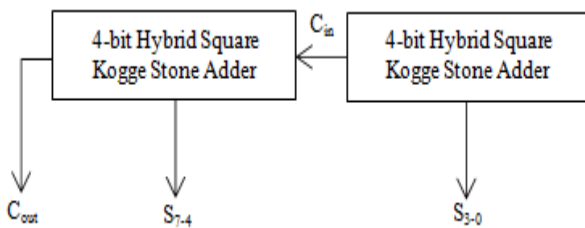


Fig 4. 8-bit Hybrid Square Kogge Stone Adder.

IV. COMPLEX MULTIPLIER

Suppose two numbers are complex then

$$A = A_r + jA_i$$

$$B = B_r + jB_i$$

The product of A and B then

$$P = A \times B$$

$$P = A_r \times B_r - A_i \times B_i + j(A_r \times B_i + A_i \times B_r)$$

$$P_r = A_r \times B_r - A_i \times B_i$$

$$P_i = A_r \times B_i + A_i \times B_r$$

Where Pr and Pi is represents the real and imaginary part of the output of the complex multiplier. Ar and Ai is represents the real and imaginary part of the first input of the complex multiplier. Br and Bi is represents the real and imaginary part of the second input of the complex multiplier.

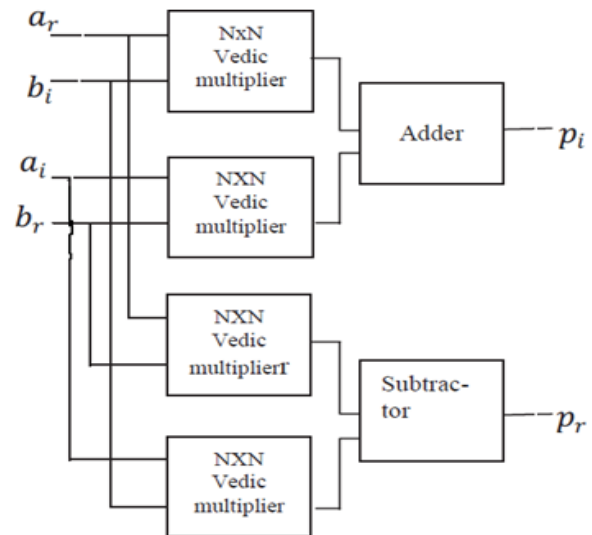


Fig 5. Block Diagram of Complex Multiplier for four Vedic Multiplier

Complex multiplier for four Vedic multipliers is shown in figure 5. In this block diagram reduce four Vedic multipliers to three Vedic multipliers is shown in below:

$$P_r = A_r \times B_r - A_i \times B_i = A_r(B_r + B_i) - B_i(A_r + A_i)$$

$$P_i = A_r \times B_i + A_i \times B_r = A_r(B_r + B_i) + B_r(A_i - A_r)$$

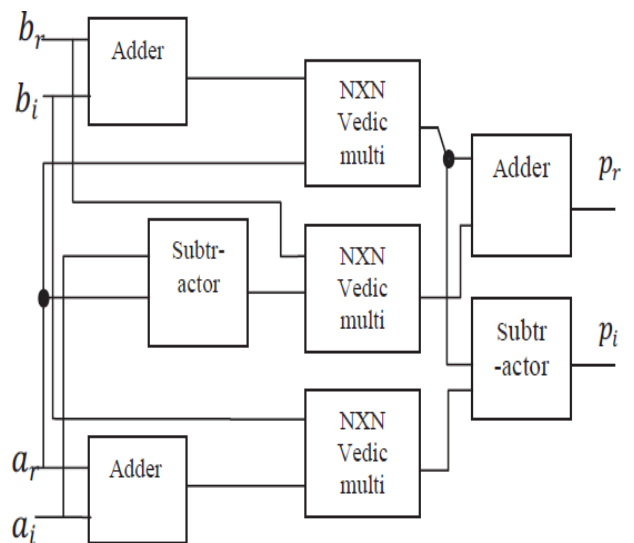


Fig 6. Block Diagram of Complex Multiplier for three Vedic Multiplier.

V. SIMULATION ANALYSIS

Simulation of these experiments can be done by using Xilinx VHDL tool. In this paper we are focusing on propagation delay. Propagation delay must be less for better performance of digital circuit.

As shown in table II the delay is obtained for the hybrid square kogge stone adder and previous algorithm. From the analysis of the results, it is found that the hybrid square kogge stone adder gives a superior performance as compared with previous algorithm for Vertex-7 device family.

Table 2. Comparison Result of Different Adder.

Word size	Adder	Delay(ns)
8-bit	Ripple Carry Adder	2.466
	Carry Select Adder	2.462
	Kogge Stone Adder	2.532
	Hybrid Square Kogge Stone	2.426
16-bit	Ripple Carry Adder	4.088
	Carry Select Adder	4.032
	Kogge Stone Adder	3.990
	Hybrid Square Kogge Stone	3.784
32-bit	Ripple Carry Adder	8.178
	Carry Select Adder	8.034
	Kogge Stone Adder	8.002
	Hybrid Square Kogge Stone	7.892
64-bit	Ripple Carry Adder	15.788
	Carry Select Adder	15.023
	Kogge Stone Adder	14.045
	Hybrid Square Kogge Stone	13.773

Table 3. Comparison Result for 8-bit Vedic Multiplier.

Design	Number of Slice	Number of LUTs	Delay
Vedic Multiplier using Full Adder [1]	111	198	-
Vedic Multiplier using Ripple Carry Adder	102	178	30.077 ns
Vedic Multiplier using Hybrid Square Kogge Stone Adder	99	171	27.180 ns

As shown in table III the number of slice, number of LUTs, delay are obtained for the Vedic multiplier using hybrid square kogge stone adder and previous algorithm. From the analysis of the results, it is found that the Vedic multiplier using hybrid square kogge stone adder gives a superior performance as compared with previous algorithm for Spartan-3 device family.

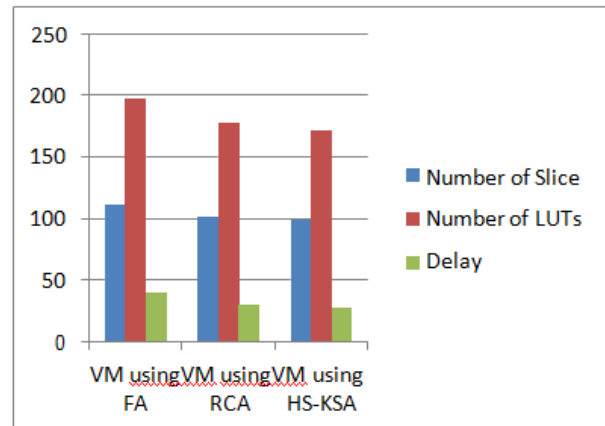


Fig 7. Bar graph of the 8-bit Vedic multiplier.

Figure 7 shows the graphical illustration of the performance of VM using KSA algorithm discussed in this research work in term of number of slice, number of LUTs and delay. From the above graphical representation it can be inferred that the VM using KSA algorithm gives the best performance as compared with previous algorithm.

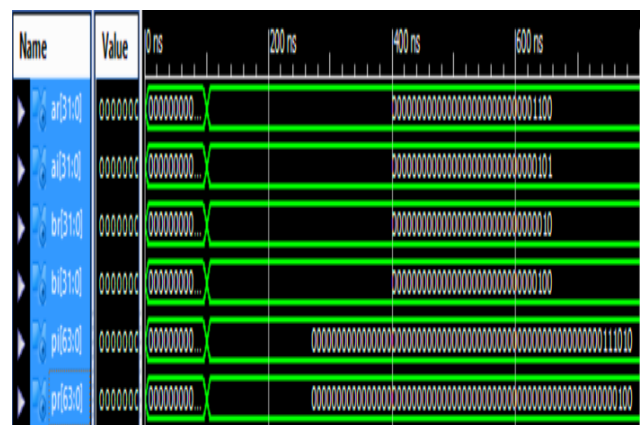


Fig 8. Output Binary Waveform of 32-bit Complex Multiplier using HS-KSA.

As shown in table IV the number of LUTs, delays are obtained for the complex Vedic multiplier using hybrid square kogge stone adder and previous algorithm. From the analysis of the results, it is found that the complex Vedic multiplier using hybrid square kogge stone adder gives a superior

performance as compared with previous algorithm for Vertex-7 device family. The output waveform of the 32-bit complex multiplier using hybrid square Kogge Stone adder is shown in figure 8 and figure 9 respectively.

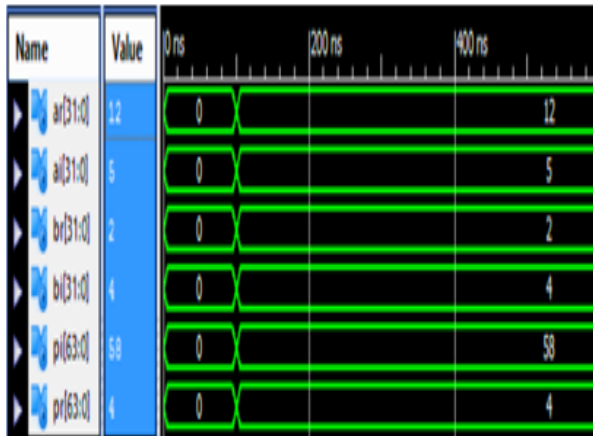


Fig 9. Output Decimal Waveform of 32-bit Complex Multiplier using HS-KSA.

Table 4. Comparison Result for 32-bit Complex Vedic Multiplier for four Vedic Multiplier.

Design	Number of LUTs	Number of IOBs	Delay
Complex Vedic Multiplier [2]	10416	256	25.979 ns
Complex Vedic Multiplier using Ripple Carry Adder	10642	256	26.927 ns
Complex Vedic Multiplier using Hybrid Square Kogge Stone Adder	10222	256	25.204 ns

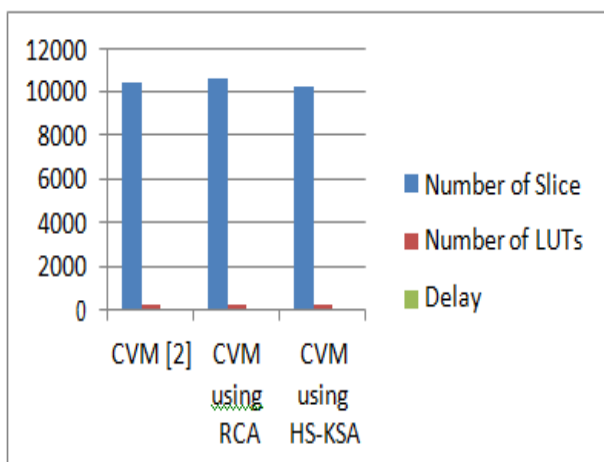


Fig 10. Bar graph of the 32-bit Complex Vedic multiplier.

Figure 10 shows the graphical illustration of the performance of CVM using KSA algorithm discussed in this research work in term of number of slice, number of LUTs and delay. From the above graphical representation it can be inferred that the CVM using KSA algorithm gives the best performance as compared with previous algorithm.

VI. CONCLUSION

In this paper design of hybrid square Kogge Stone adder, Vedic multiplier and complex Vedic multiplier is presented. From implementation results it is observed that the hybrid based Vedic Multiplier and complex Vedic multiplier consumes less delay compare to previous design.

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